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PRACTICE PAPER 01 (2023-24)
ALGEBRAIC EXPRESSIONS AND IDENTITIES
(ANSWERS)

SUBJECT: MATHEMATICS
CLASS : VIII

MAX. MARKS : 30
DURATION : 1 hr

SECTION – A (1 mark)

1. Add $7x^2 + 11x + 8$ and $3x^2 - 6x - 7$.
Ans: $(7x^2 + 11x + 8) + (3x^2 - 6x - 7)$
 $= (7x^2 + 3x^2) + (11x - 6x) + (8 - 7)$
 $= 10x^2 + 5x + 1$
2. Find the product of $5x^2y$ and $-3x^3y^2$.
Ans: $(5x^2y)(-3x^3y^2) = 5(-3)(x^2x^3)(y.y^2)$
 $= -15x^{2+3}y^{1+2} = -15x^5y^3$
3. Find the product of a^4b^2 and $(2a^2b)^3$.
Ans: $(a^4b^2)(2a^2b)^3 = (a^4b^2)[2^3(a^2)^3.b^3]$
 $= 8(a^4.a^6).(b^2.b^3) = 8a^{10}b^5$
4. Find the product of $3x$ and $7x + 2$.
Ans: Product = $3x(7x + 2)$
 $= (3x)(7x) + (3x)(2) = 21x^2 + 6x.$
5. Find the product of $-5m^2$ and $4m^2 - 2m + 7$.
Ans: Product = $-5m^2(4m^2 - 2m + 7)$
 $= (-5m^2)(4m^2) + (-5m^2)(-2m) + (-5m^2)(7)$
 $= -20m^4 + 10m^3 - 35m^2$

SECTION – B (2 marks)

6. Simplify: $5x^3 + 6x^2 + 3x - (-2x^3 + 7x^2 + 3x - 7)$
Ans: $5x^3 + 6x^2 + 3x - (-2x^3 + 7x^2 + 3x - 7)$
 $= 5x^3 + 6x^2 + 3x + 2x^3 - 7x^2 - 3x + 7$
 $= (5x^3 + 2x^3) + (6x^2 - 7x^2) + (3x - 3x) + 7$
 $= 7x^3 - x^2 + 7$
7. Add $3x(7x^2 - 5x + 3)$ and $2(x^3 - 4x^2 + 5)$.
Ans: $3x(7x^2 - 5x + 3) + 2(x^3 - 4x^2 + 5)$
 $= 21x^3 - 15x^2 + 9x + 2x^3 - 8x^2 + 10$
 $= 21x^3 - 2x^3 - 15x^2 - 8x^2 + 9x + 10$
 $= 23x^3 - 23x^2 + 9x + 10$

8. Multiply $2a + 3b$ by $7a - 5b$.

$$\begin{aligned}\text{Ans: Product} &= (2a + 3b)(7a - 5b) \\ &= 2a(7a - 5b) + 3b(7a - 5b) \\ &= 14a^2 - 10ab + 21ab - 15b^2 \\ &= 14a^2 + 11ab - 15b^2.\end{aligned}$$

9. Multiply : $(5a^2 - 2b)$ by $(2a^2 - 3b)$.

$$\begin{aligned}\text{Ans: Product} &= (5a^2 - 2b)(2a^2 - 3b) \\ &= 5a^2(2a^2 - 3b) - 2b(2a^2 - 3b) \\ &= 10a^4 - 15a^2b - 4a^2b + 6b^2 \\ &= 10a^4 - 19a^2b + 6b^2\end{aligned}$$

10. Find the Square of $9x - 7xy$.

$$\begin{aligned}\text{Ans: As per the condition in the question, } &(9x - 7xy)^2 \\ \text{The standard identity} &= (a - b)^2 = a^2 - 2ab + b^2 \\ \text{Where, } a &= 9x, b = 7xy \\ \text{Then, } (9x - 7xy)^2 &= (9x)^2 - (2 \times 9x \times 7xy) + (7xy)^2 \\ &= 81x^2 - 126x^2y + 49x^2y^2\end{aligned}$$

SECTION – C (3 marks)

11. Simplify : $a^2(b^2 - c^2) + b^2(c^2 - a^2) + c^2(a^2 - b^2)$

$$\begin{aligned}\text{Ans: } &a^2(b^2 - c^2) + b^2(c^2 - a^2) + c^2(a^2 - b^2) \\ &= (a^2b^2 - a^2c^2) + (b^2c^2 - b^2a^2) + (c^2a^2 - c^2b^2) \\ &= (a^2b^2 - b^2a^2) + (-a^2c^2 + c^2a^2) + (b^2c^2 - c^2b^2) \\ &= (a^2b^2 - a^2b^2) + (-c^2a^2 + c^2a^2) + (b^2c^2 - b^2c^2) \\ &= 0 + 0 + 0 = 0.\end{aligned}$$

12. Subtract $4p^2q - 3pq + 5pq^2 - 8p + 7q - 10$ from $18 - 3p - 11q + 5pq - 2pq^2 + 5p^2q$

$$\begin{aligned}\text{Ans: } &(18 - 3p - 11q + 5pq - 2pq^2 + 5p^2q) - (4p^2q - 3pq + 5pq^2 - 8p + 7q - 10) \\ &= 18 - 3p - 11q + 5pq - 2pq^2 + 5p^2q - 4p^2q + 3pq - 5pq^2 + 8p - 7q + 10 \\ &= 18 + 10 - 3p + 8p - 11q - 7q + 5pq + 3pq - 2pq^2 - 5pq^2 + 5p^2q - 4p^2q \\ &= 28 + 5p - 18q + 8pq - 7pq^2 + p^2q\end{aligned}$$

13. Use the identity $(x + a)(x + b) = x^2 + (a + b)x + ab$ to find the following products.

(i) $(4x + 5)(4x - 1)$ (ii) $(2x + 5y)(2x + 3y)$

$$\begin{aligned}\text{Ans: (i) } &(4x + 5)(4x - 1) \\ &= 16x^2 + [5 + (-1)]4x + 5(-1) \\ &= 16x^2 + 16x - 5 \\ \text{(ii) } &(2x + 5y)(2x + 3y) \\ &= 4x^2 + (5y + 3y)2x + (5y)(3y) \\ &= 4x^2 + 16xy + 15y^2\end{aligned}$$

14. Use a suitable identity to get each of the following products.

(i) $(2y + 5)(2y + 5)$ (ii) $(2a - 7)(2a - 7)$

$$\begin{aligned}\text{Ans: (i) } &(2y + 5)(2y + 5) = (2y + 5)^2 \\ &= 4y^2 + 20y + 25\end{aligned}$$

Using $(a + b)^2 = a^2 + b^2 + 2ab$

$$(ii) (2a - 7)(2a - 7) = (2a - 7)^2$$

$$= 4a^2 - 28a + 49$$

Using $(a - b)^2 = a^2 + b^2 - 2ab$

15. Simplify the following expression and evaluate it for $a = -1$.

$$5a^2(a - 2) - 2a^3(a + 4) - 5a(a - 2)$$

$$\text{Ans: } 5a^2(a - 2) - 2a^3(a + 4) - 5a(a - 2)$$

$$= [5a^2 \times a - 5a^2 \times 2] - [2a^3 \times a + 2a^3 \times 4] - [5a \times a - 5a \times 2]$$

$$= (5a^3 - 10a^2) - (2a^4 + 8a^3) - (5a^2 - 10a)$$

$$= 5a^3 - 10a^2 - 2a^4 - 8a^3 - 5a^2 + 10a$$

$$= -2a^4 - 3a^3 - 15a^2 + 10a$$

$$= -2(-1)^4 - 3(-1)^3 - 15(-1)^2 + 10(-1) \quad [\text{Putting } a = -1]$$

$$= -2 + 3 - 15 - 10 = -27 + 3 = -24$$