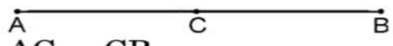


SESSION ENDING EXAMINATION 2023-24

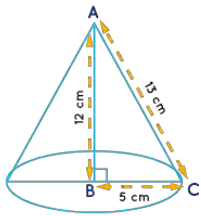
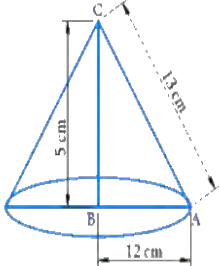
Class – IX

Marking Scheme

Subject - Mathematics

S. No.	Section A	Marks																																		
	Section A consists of 20 questions of 1 mark each																																			
1	D	1																																		
2	D	1																																		
3	C	1																																		
4	B	1																																		
5	B	1																																		
6	A	1																																		
7	C	1																																		
8	D	1																																		
9	A	1																																		
10	B	1																																		
11	C	1																																		
12	B	1																																		
13	B	1																																		
14	A	1																																		
15	B	1																																		
16	A	1																																		
17	B	1																																		
18	C	1																																		
19	A	1																																		
20	A	1																																		
Section B consists of 5 questions of 2 marks each																																				
21	493 cm cube (nearly) (correct formula, correct calculation, correct answer) 3845.44 g(nearly)	1+1																																		
22	$[(2x - (2x - y)] \{(2x)^2 + 2x(2x - y) + (2x - y)^2\}$ $y(12x^2 - 6xy + y^2)$	1+1																																		
23	(0,0) (0,-4)	1 + 1																																		
24	 <p>AC = CB Also AC + AC = BC + AC. (Equals are added to equals) BC + AC coincides with AB ⇒ 2AC = AB ⇒ AC = $\frac{1}{2}$ AB.</p> <p>Or Correct explanation</p>	1 1 2																																		
25	<table border="1" style="width:100%; border-collapse: collapse;"> <tr> <td style="width:25%;">$\frac{S_1}{S_2} = \frac{4\pi r_1^2}{4\pi r_2^2}$</td> <td style="width:10%; text-align:center;">½</td> <td rowspan="2" style="width:10%; text-align:center;">OR</td> <td style="width:25%;">$r = \sqrt{l^2 - h^2}$</td> <td style="width:10%;"></td> </tr> <tr> <td>$\frac{1}{4} = \frac{r_1^2}{r_2^2}$</td> <td></td> <td>$r = \sqrt{169 - 144} = \sqrt{25}$</td> <td></td> </tr> <tr> <td>$\frac{r_1}{r_2} = \frac{1}{2}$</td> <td style="text-align:center;">½</td> <td></td> <td>$r = 5$ cm</td> <td style="text-align:center;">½</td> </tr> <tr> <td>$\frac{V_1}{V_2} = \frac{\frac{4}{3}\pi r_1^3}{\frac{4}{3}\pi r_2^3} = \frac{r_1^3}{r_2^3}$</td> <td></td> <td></td> <td>$V = \frac{1}{3} \pi r^2 h$</td> <td style="text-align:center;">½</td> </tr> <tr> <td>$(\frac{1}{2})^3 \frac{V_1}{V_2} = \frac{1}{8}$</td> <td style="text-align:center;">½</td> <td></td> <td>$V = \frac{1}{3} \times \frac{22}{7} \times 5 \times 5 \times 12$</td> <td style="text-align:center;">½</td> </tr> <tr> <td></td> <td></td> <td></td> <td>$V = 314.28$ cm³</td> <td></td> </tr> <tr> <td></td> <td></td> <td></td> <td>$V = 0.31428$ litres</td> <td style="text-align:center;">½</td> </tr> </table>	$\frac{S_1}{S_2} = \frac{4\pi r_1^2}{4\pi r_2^2}$	½	OR	$r = \sqrt{l^2 - h^2}$		$\frac{1}{4} = \frac{r_1^2}{r_2^2}$		$r = \sqrt{169 - 144} = \sqrt{25}$		$\frac{r_1}{r_2} = \frac{1}{2}$	½		$r = 5$ cm	½	$\frac{V_1}{V_2} = \frac{\frac{4}{3}\pi r_1^3}{\frac{4}{3}\pi r_2^3} = \frac{r_1^3}{r_2^3}$			$V = \frac{1}{3} \pi r^2 h$	½	$(\frac{1}{2})^3 \frac{V_1}{V_2} = \frac{1}{8}$	½		$V = \frac{1}{3} \times \frac{22}{7} \times 5 \times 5 \times 12$	½				$V = 314.28$ cm ³					$V = 0.31428$ litres	½	1+1
$\frac{S_1}{S_2} = \frac{4\pi r_1^2}{4\pi r_2^2}$	½	OR	$r = \sqrt{l^2 - h^2}$																																	
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			$V = 0.31428$ litres	½																																
Section C consists of 6 questions of 3 marks each																																				

26	<p>Solution</p> <p>Given, $x - \frac{1}{x} = 5$</p> <p>Squaring both the sides,</p> $\Rightarrow \left(x - \frac{1}{x}\right)^2 = 5^2$ $\Rightarrow x^2 + \frac{1}{x^2} - 2\left(x\right)\left(\frac{1}{x}\right) = 25$ $\Rightarrow x^2 + \frac{1}{x^2} = 25 + 2$ $\Rightarrow x^2 + \frac{1}{x^2} = 27$ <p>Now,</p> $x^3 - \frac{1}{x^3}$ $= \left(x - \frac{1}{x}\right) \left[\left(x\right)^2 + \left(\frac{1}{x}\right)^2 + \left(x\right)\left(\frac{1}{x}\right) \right]$ $= 5(27 + 1)$ $= 140$	1 1 1
	<p>or</p> $P(x) = x^3 - 23x^2 + 142x - 120$ <p>$P(1) = 0$, $(x-1)$ is factor of $p(x)$</p> $P(x) = x^2(x-1) - 22x(x-1) + 120(x-1)$ $= (x-1)(x^2 - 22x + 120)$ $= (x-1)(x-10)(x-12)$	1 1 1
27	For correct representation + construction	1+2
28	For correct diagram For correct proof	1 2
29	<p>For correct figure For correct proof OR In ΔAMC and ΔBMD $AM=BM$ (M is midpoint of AB) $\angle AMC=\angle BMD$(vertically opposite angles) $CM=DM$ (given) $\therefore \Delta AMC \cong \Delta BMD$ (by SAS congruence rule) $\therefore AC=BD$ (by CPCT) $\Rightarrow \angle DBC + \angle ACB = 180^\circ$ (co-interior angles) $\Rightarrow \angle DBC + 90^\circ = 180^\circ$ ($\angle ACB = 90^\circ$) $\Rightarrow \angle DBC = 180^\circ - 90^\circ \Rightarrow \angle DBC = 90^\circ$ $\Rightarrow DB=AC$ (By CPCT)...(i) In ΔDBC and ΔACB $DB=AC$ (From (i)) $BC=BC$ (Common) $\angle DBC = \angle ACB = 90^\circ$ $\therefore \Delta DBC \cong \Delta ACB$ by SAS congruence</p>	1 2 1+1+1
30	<p>i) $375\sqrt{15}m^2$ (Using correct formula + correct calculation + correct answer) ii) $900\sqrt{3}m^2$ (Using correct formula + correct calculation + correct answer)</p>	$\frac{1}{2}$ + $\frac{1}{2}$ + $\frac{1}{2}$ $\frac{1}{2}$ + $\frac{1}{2}$ + $\frac{1}{2}$
31	For 3 correct solutions	1+1+1
Section D		
Section D consists of 4 questions of 5 marks each		
32	<p>i) $\angle POS + \angle SOQ = 180^\circ$ $\angle ROT = 90^\circ$</p> <p>ii) Since BE and FC are normal to PQ and RS respectively, therefore, $BE \parallel FC$ Let, $\angle ABE = \angle EBC = x$ [PQ is a mirror, so angle of incidence is equal to angle of reflection] $\angle FCD = \angle BCF = y$ [RS is a mirror, so angle of incidence is equal to angle of reflection] Now considering BE and FC, taking BC as transversal,</p>	1 1 .5 .5

	$\angle EBC = \angle BCF \dots \dots (i)$ [alternate interior angle] i.e. $x = y$ i.e. $\angle ABE = \angle FCD \dots \dots (ii)$ Adding equation (i) and (ii) $\angle EBC + \angle ABE = \angle BCF + \angle FCD$ $\angle ABC = \angle BCD$ Now if we take line AB and CD in consideration, alternate interior angles that are $\angle ABC$ and $\angle BCD$ are equal. Therefore, $AB \parallel CD$.5 .5 .5 .5
33	find Slant height = 25 m (Using correct formula + correct calculation + correct answer) find height = 24 m (Using correct formula + correct calculation + correct answer) volume of the tent $1232m^3$ (Using correct formula + correct calculation + correct answer) or (a) Since the triangle is revolved about the side 12 cm, a solid <u>cone</u> is formed with a height of 12 cm and radius of the base of 5 cm as shown below. <u>Volume of a cone</u> having radius 'r', and height 'h', = $\frac{1}{3}\pi r^2 h$ Radius of the cone, 'r' = 5 cm Height of the cone, 'h' = 12 cm Volume of the cone = $\frac{1}{3}\pi r^2 h$ = $\frac{1}{3} \times \pi \times 5 \text{ cm} \times 5 \text{ cm} \times 12 \text{ cm}$ = $100\pi \text{ cm}^3$ Volume of the cone is $100\pi \text{ cm}^3$. (b) Since the triangle is revolved about the side 5 cm, solid <u>cone</u> is formed with a height of 5 cm and radius of the base of 12 cm. <u>Volume of a cone</u> having radius 'r' and height 'h' = $\frac{1}{3}\pi r^2 h$ Radius of the cone, $r = 12 \text{ cm}$ Height of the cone, $h = 5 \text{ cm}$ Volume of the cone = $\frac{1}{3}\pi r^2 h$ = $(\frac{1}{3}) \times \pi \times 12 \text{ cm} \times 12 \text{ cm} \times 5 \text{ cm}$ = $240\pi \text{ cm}^3$ (c) Ratio = Volume of the cone in (a) / Volume of the cone in (b) = $100\pi : 240\pi$ = 5 : 12 The volume of the cone is $240\pi \text{ cm}^3$ and the required ratio is 5 : 12	1+1 1 2 2 2 1 1
	 	base of a of the

34	1 mark for each part Or For correct figure (i) In $\triangle ACB$, M is the midpoint of AB and $MD \parallel BC$	1
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	D is the midpoint of AC (Converse of mid point theorem) (ii) $\angle ACB = \angle ADM$ (Corresponding angles) also, $\angle ACB = 90^\circ$ $\angle ADM = 90^\circ$ and $MD \perp AC$ (iii) In $\triangle AMD$ and $\triangle CMD$, $AD = CD$ (D is the midpoint of side AC) $\angle ADM = \angle CDM$ (Each 90°) $DM = DM$ (common) $\triangle AMD \cong \triangle CMD$ [SAS congruency] $AM = CM$ [CPCT] also, $AM = \frac{1}{2} AB$ (M is midpoint of AB) Hence, $CM = MA = \frac{1}{2} AB$	1 1 1 1
35	For making class interval continuous For class mark+ proper scaling frequency polygon	1 1+1/2 2 1/2
Section E		
Section E consists of 3 questions of 4 marks each		
36	a) degree is 2 , Quadratic polynomial b) Linear c) $(2x+1), (2x-5)$ or 39195	$\frac{1}{2} + \frac{1}{2}$ 1 2
37	(a) Angle QPR = 90 degree (b) Triangle QPR is a right angled triangle $4r^2 = 64 + 36$ $r = 5$ cm OR Perimeter of circle = $2\pi r$ $= 2 \times \frac{22}{7} \times 5 = 31.4$ cm (c) Angle QSR = Angle QPR = 90 degree (Angle in the same segment)	1 2 1
38	i) $\sqrt{3} - \sqrt{2}$ ii) Rational iii) $22 - 4\sqrt{28}$ Or $\sqrt{77} - \sqrt{35}$ ----- 6	1 1 2