

6

Trigonometry



Let's study.

- Trigonometric ratios
- Trigonometric identities
- Angle of elevation and angle of depression
- Problems based on heights and distances



Let's recall.

1. Fill in the blanks with reference to figure 6.1 .

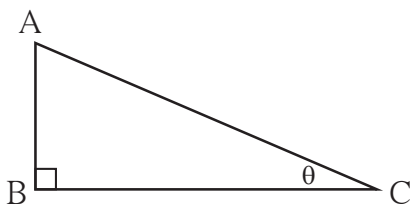


Fig. 6.1

$$\sin \theta = \frac{\boxed{}}{\boxed{}}, \cos \theta = \frac{\boxed{}}{\boxed{}},$$

$$\tan \theta = \frac{\boxed{}}{\boxed{}}$$

2. Complete the relations in ratios given below .

- (i) $\frac{\sin \theta}{\cos \theta} = \boxed{}$ (ii) $\sin \theta = \cos (90 - \boxed{})$
 (iii) $\cos \theta = \sin (90 - \boxed{})$ (iv) $\tan \theta \times \tan (90 - \theta) = \boxed{}$

3. Complete the equation.

$$\sin^2 \theta + \cos^2 \theta = \boxed{}$$

4. Write the values of the following trigonometric ratios.

- (i) $\sin 30^\circ = \frac{1}{\boxed{}}$ (ii) $\cos 30^\circ = \frac{\boxed{}}{\boxed{}}$ (iii) $\tan 30^\circ = \frac{\boxed{}}{\boxed{}}$
 (iv) $\sin 60^\circ = \frac{\boxed{}}{\boxed{}}$ (v) $\cos 45^\circ = \frac{\boxed{}}{\boxed{}}$ (vi) $\tan 45^\circ = \boxed{}$

In std IX, we have studied some trigonometric ratios of some acute angles.

Now we are going to study some more trigonometric ratios of acute angles.



Let's learn.

cosec, sec and cot ratios

Multiplicative inverse or the reciprocal of sine ratio is called cosecant ratio. It is written in brief as cosec. $\therefore \text{cosec}\theta = \frac{1}{\sin\theta}$

Similarly, multiplicative inverses or reciprocals of cosine and tangent ratios are called “secant” and “cotangent” ratios respectively. They are written in brief as sec and cot.

$$\therefore \sec\theta = \frac{1}{\cos\theta} \quad \text{and} \quad \cot\theta = \frac{1}{\tan\theta}$$

In figure 6.2,

$$\sin\theta = \frac{AB}{AC}$$

$$\begin{aligned} \therefore \text{cosec}\theta &= \frac{1}{\sin\theta} \\ &= \frac{1}{\frac{AB}{AC}} \\ &= \frac{AC}{AB} \end{aligned}$$

It means,

$$\text{cosec}\theta = \frac{\text{hypotenuse}}{\text{opposite side}}$$

$$\tan\theta = \frac{AB}{BC}$$

$$\begin{aligned} \therefore \cot\theta &= \frac{1}{\tan\theta} \\ &= \frac{1}{\frac{AB}{BC}} \end{aligned}$$

$$\cot\theta = \frac{BC}{AB} = \frac{\text{adjacent side}}{\text{opposite side}}$$

$$\cos\theta = \frac{BC}{AC}$$

$$\begin{aligned} \sec\theta &= \frac{1}{\cos\theta} \\ &= \frac{1}{\frac{BC}{AC}} \\ &= \frac{AC}{BC} \end{aligned}$$

It means,

$$\sec\theta = \frac{\text{hypotenuse}}{\text{adjacent side}}$$

You know that,

$$\tan\theta = \frac{\sin\theta}{\cos\theta}$$

$$\begin{aligned} \therefore \cot\theta &= \frac{1}{\tan\theta} \\ &= \frac{1}{\frac{\sin\theta}{\cos\theta}} \end{aligned}$$

$$= \frac{\cos\theta}{\sin\theta}$$

$$\therefore \cot\theta = \frac{\cos\theta}{\sin\theta}$$

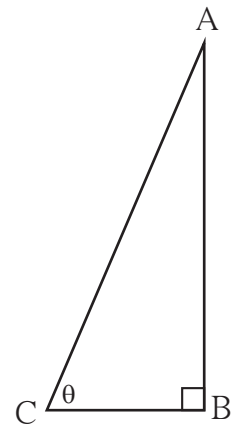


Fig. 6.2



Remember this!

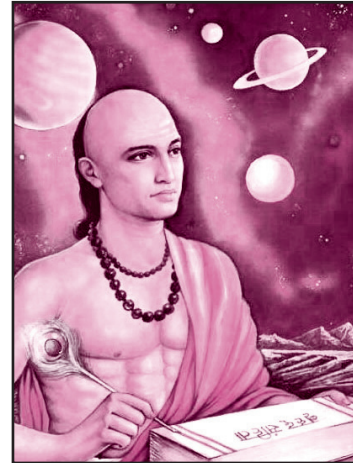
The relation between the trigonometric ratios, according to the definitions of cosec, sec and cot ratios

- $\frac{1}{\sin \theta} = \operatorname{cosec} \theta \quad \therefore \sin \theta \times \operatorname{cosec} \theta = 1$
- $\frac{1}{\cos \theta} = \sec \theta \quad \therefore \cos \theta \times \sec \theta = 1$
- $\frac{1}{\tan \theta} = \cot \theta \quad \therefore \tan \theta \times \cot \theta = 1$

For more information :

The great Indian mathematician Aryabhata was born in 476 A.D. in Kusumpur which was near Patna in Bihar. He has done important work in Arithmetic, Algebra and Geometry. In the book ‘Aryabhatiya’ he has written many mathematical formulae. For example,

- (1) In an Arithmetic Progression, formulae for n^{th} term and the sum of first n terms.
- (2) The formula to approximate $\sqrt{2}$
- (3) The correct value of π upto four decimals, $\pi = 3.1416$.



In the study of Astronomy he used trigonometry and the sine ratio of an angle for the first time.

Comparing with the mathematics in the rest of the world at that time, his work was great and was studied all over India and was carried to Europe through Middle East.

Most observers at that time believed that the earth is immovable and the Sun, the Moon and stars move around the earth. But Aryabhata noted that when we travel in a boat on the river, objects like trees, houses on the bank appear to move in the opposite direction. ‘Similarly’, he said ‘the Sun, Moon and the stars are observed by people on the earth to be moving in the opposite direction while in reality the Earth moves !’

On 19 April 1975, India sent the first satellite in the space and it was named ‘Aryabhata’ to commemorate the great Mathematician of India.

* The table of the values of trigonometric ratios of angles $0^\circ, 30^\circ, 45^\circ, 60^\circ$ and 90° .

Trigonometric ratio	Angle (θ)				
	0°	30°	45°	60°	90°
$\sin \theta$	0	$\frac{1}{2}$	$\frac{1}{\sqrt{2}}$	$\frac{\sqrt{3}}{2}$	1
$\cos \theta$	1	$\frac{\sqrt{3}}{2}$	$\frac{1}{\sqrt{2}}$	$\frac{1}{2}$	0
$\tan \theta$	0	$\frac{1}{\sqrt{3}}$	1	$\sqrt{3}$	Not defined
$\operatorname{cosec} \theta$ $= \frac{1}{\sin \theta}$	Not defined	2	$\sqrt{2}$	$\frac{2}{\sqrt{3}}$	1
$\sec \theta$ $= \frac{1}{\cos \theta}$	1	$\frac{2}{\sqrt{3}}$	$\sqrt{2}$	2	Not defined
$\cot \theta$ $= \frac{1}{\tan \theta}$	Not defined	$\sqrt{3}$	1	$\frac{1}{\sqrt{3}}$	0



Trigonometric identities

In the figure 6.3, ΔABC is a right angled triangle, $\angle B = 90^\circ$

- (i) $\sin \theta = \frac{BC}{AC}$ (ii) $\cos \theta = \frac{AB}{AC}$
 (iii) $\tan \theta = \frac{BC}{AB}$ (iv) $\operatorname{cosec} \theta = \frac{AC}{BC}$
 (v) $\sec \theta = \frac{AC}{AB}$ (vi) $\cot \theta = \frac{AB}{BC}$

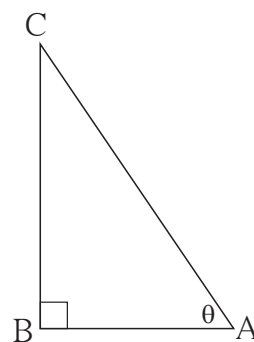


Fig. 6.3

By Pythagoras theorem,

$$BC^2 + AB^2 = AC^2 \dots\dots(I)$$

Dividing both the sides of (1) by AC^2

$$\frac{BC^2 + AB^2}{AC^2} = \frac{AC^2}{AC^2}$$

$$\therefore \frac{BC^2}{AC^2} + \frac{AB^2}{AC^2} = 1$$

$$\therefore \left(\frac{BC}{AC}\right)^2 + \left(\frac{AB}{AC}\right)^2 = 1$$

$\therefore (\sin\theta)^2 + (\cos\theta)^2 = 1$ [(sin θ)² is written as sin² θ and (cos θ)² is written as cos² θ .]

$$\sin^2\theta + \cos^2\theta = 1 \dots\dots\dots \text{(II)}$$

Now dividing both the sides of equation (II) by sin² θ

$$\frac{\sin^2\theta}{\sin^2\theta} + \frac{\cos^2\theta}{\sin^2\theta} = \frac{1}{\sin^2\theta}$$

$$1 + \cot^2\theta = \operatorname{cosec}^2\theta \dots\dots\dots \text{(III)}$$

Dividing both the sides of equation (II) by cos² θ

$$\frac{\sin^2\theta}{\cos^2\theta} + \frac{\cos^2\theta}{\cos^2\theta} = \frac{1}{\cos^2\theta}$$

$$\tan^2\theta + 1 = \sec^2\theta$$

$$1 + \tan^2\theta = \sec^2\theta \dots\dots\dots \text{(IV)}$$

Relations (II),(III), and (IV) are fundamental trigonometric identities.

Solved Examples

Ex. (1) If $\sin\theta = \frac{20}{29}$ then find $\cos\theta$

Solution : **Method I**

We have

$$\sin^2\theta + \cos^2\theta = 1$$

$$\left(\frac{20}{29}\right)^2 + \cos^2\theta = 1$$

$$\frac{400}{841} + \cos^2\theta = 1$$

$$\cos^2\theta = 1 - \frac{400}{841}$$

$$= \frac{441}{841}$$

Taking square root of both sides.

$$\cos\theta = \frac{21}{29}$$

Method II

$$\sin\theta = \frac{20}{29}$$

from figure, $\sin\theta = \frac{AB}{AC}$

$$\therefore AB = 20k \text{ and } AC = 29k$$

Let $BC = x$.

According to Pythagoras therom,

$$AB^2 + BC^2 = AC^2$$

$$(20k)^2 + x^2 = (29k)^2$$

$$400k^2 + x^2 = 841k^2$$

$$x^2 = 841k^2 - 400k^2$$

$$= 441k^2$$

$$\therefore x = 21k$$

$$\therefore \cos\theta = \frac{BC}{AC} = \frac{21k}{29k} = \frac{21}{29}$$

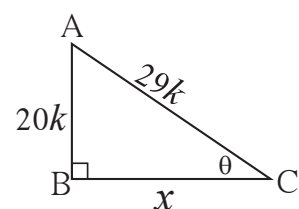


Fig. 6.4

Ex. (4) $\cos\theta = \frac{\sqrt{3}}{2}$ then find the value of $\frac{1-\sec\theta}{1+\operatorname{cosec}\theta}$.

Solution : **Method I**

$$\cos\theta = \frac{\sqrt{3}}{2} \quad \therefore \sec\theta = \frac{2}{\sqrt{3}}$$

$$\sin^2\theta + \cos^2\theta = 1$$

$$\therefore \sin^2\theta + \left(\frac{\sqrt{3}}{2}\right)^2 = 1$$

$$\therefore \sin^2\theta = 1 - \frac{3}{4} = \frac{1}{4}$$

$$\therefore \sin\theta = \frac{1}{2} \quad \therefore \operatorname{cosec}\theta = 2$$

$$\therefore \frac{1-\sec\theta}{1+\operatorname{cosec}\theta} = \frac{1-\frac{2}{\sqrt{3}}}{1+2}$$

$$= \frac{\frac{\sqrt{3}-2}{\sqrt{3}}}{3}$$

$$= \frac{\sqrt{3}-2}{3\sqrt{3}}$$

Method II

$$\cos\theta = \frac{\sqrt{3}}{2}$$

we know that, $\cos 30^\circ = \frac{\sqrt{3}}{2}$.

$$\therefore \theta = 30^\circ$$

$$\therefore \sec\theta = \sec 30^\circ = \frac{2}{\sqrt{3}}$$

$$\operatorname{cosec}\theta = \operatorname{cosec} 30^\circ = 2$$

$$\therefore \frac{1-\sec\theta}{1+\operatorname{cosec}\theta} = \frac{1-\frac{2}{\sqrt{3}}}{1+2}$$

$$= \frac{\frac{\sqrt{3}-2}{\sqrt{3}}}{3}$$

$$= \frac{\sqrt{3}-2}{3\sqrt{3}}$$

Ex. (5) Show that $\sec x + \tan x = \sqrt{\frac{1+\sin x}{1-\sin x}}$

Solution : $\sec x + \tan x = \frac{1}{\cos x} + \frac{\sin x}{\cos x}$

$$= \frac{1+\sin x}{\cos x}$$

$$= \sqrt{\frac{(1+\sin x)^2}{\cos^2 x}}$$

$$= \sqrt{\frac{(1+\sin x)(1+\sin x)}{1-\sin^2 x}}$$

$$= \sqrt{\frac{(1+\sin x)(1+\sin x)}{(1-\sin x)(1+\sin x)}}$$

$$= \sqrt{\frac{1+\sin x}{1-\sin x}}$$



Ex. (6) Eliminate θ from given equations.

$$x = a \cot \theta - b \operatorname{cosec} \theta$$

$$y = a \cot \theta + b \operatorname{cosec} \theta$$

Solution : $x = a \cot \theta - b \operatorname{cosec} \theta$ (I)

$$y = a \cot \theta + b \operatorname{cosec} \theta$$
 (II)

Adding equations (I) and (II).

$$x + y = 2a \cot \theta$$

$$\therefore \cot \theta = \frac{x + y}{2a}$$
 (III)

Subtracting equation (II) from (I) ,

$$y - x = 2b \operatorname{cosec} \theta$$

$$\therefore \operatorname{cosec} \theta = \frac{y - x}{2b}$$
 (IV)

$$\text{Now, } \operatorname{cosec}^2 \theta - \cot^2 \theta = 1$$

$$\therefore \left(\frac{y - x}{2b} \right)^2 - \left(\frac{y + x}{2a} \right)^2 = 1$$

$$\therefore \frac{(y - x)^2}{4b^2} - \frac{(y + x)^2}{4a^2} = 1$$

$$\text{or } \left(\frac{y - x}{b} \right)^2 - \left(\frac{y + x}{a} \right)^2 = 4$$

Practice set 6.1

1. If $\sin \theta = \frac{7}{25}$, find the values of $\cos \theta$ and $\tan \theta$.
2. If $\tan \theta = \frac{3}{4}$, find the values of $\sec \theta$ and $\cos \theta$.
3. If $\cot \theta = \frac{40}{9}$, find the values of $\operatorname{cosec} \theta$ and $\sin \theta$.
4. If $5 \sec \theta - 12 \operatorname{cosec} \theta = 0$, find the values of $\sec \theta$, $\cos \theta$ and $\sin \theta$.
5. If $\tan \theta = 1$ then, find the values of $\frac{\sin \theta + \cos \theta}{\sec \theta + \operatorname{cosec} \theta}$.
6. Prove that:
 - (1) $\frac{\sin^2 \theta}{\cos \theta} + \cos \theta = \sec \theta$
 - (2) $\cos^2 \theta (1 + \tan^2 \theta) = 1$

$$(3) \sqrt{\frac{1-\sin\theta}{1+\sin\theta}} = \sec\theta - \tan\theta$$

$$(4) (\sec\theta - \cos\theta)(\cot\theta + \tan\theta) = \tan\theta \sec\theta$$

$$(5) \cot\theta + \tan\theta = \operatorname{cosec}\theta \sec\theta$$

$$(6) \frac{1}{\sec\theta - \tan\theta} = \sec\theta + \tan\theta$$

$$(7) \sin^4\theta - \cos^4\theta = 1 - 2\cos^2\theta$$

$$(8) \sec\theta + \tan\theta = \frac{\cos\theta}{1-\sin\theta}$$

$$(9) \text{ If } \tan\theta + \frac{1}{\tan\theta} = 2, \text{ then show that } \tan^2\theta + \frac{1}{\tan^2\theta} = 2$$

$$(10) \frac{\tan A}{(1+\tan^2 A)^2} + \frac{\cot A}{(1+\cot^2 A)^2} = \sin A \cos A$$

$$(11) \sec^4 A (1 - \sin^4 A) - 2\tan^2 A = 1$$

$$(12) \frac{\tan\theta}{\sec\theta - 1} = \frac{\tan\theta + \sec\theta + 1}{\tan\theta + \sec\theta - 1}$$



Let's learn.

Application of trigonometry

Many times we need to know the height of a tower, building, tree or distance of a ship from the lighthouse or width of a river etc.

We cannot measure them actually but we can find them with the help of trigonometric ratios.

For the purpose of computation, we draw a rough sketch to show the given information. 'Trees', 'hills' or 'towers' are vertical objects, so we shall represent them in the figure by segments which are perpendicular to the ground. We will not consider height of the observer and we shall normally regard observer's line of vision to be parallel to the horizontal level.

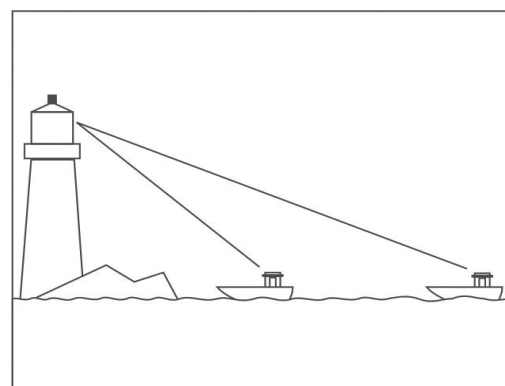


Fig. 6.6

Let us study a few related terms.

(i) **Line of vision** : If the observer is standing at the location 'A', looking at an object 'B' then the line AB is called line of the vision.

(ii) **Angle of elevation** :

If an observer at A, observes the point B which is at a level higher than A and AM is the horizontal line, then $\angle BAM$ is called the angle of elevation.

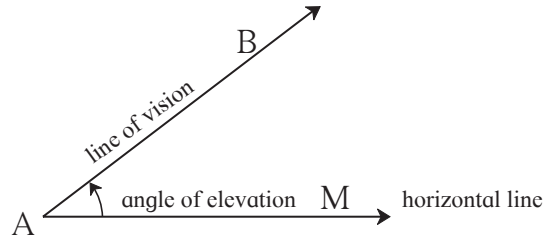


Fig. 6.7

(iii) **Angle of depression** :

If an observer at A, observes the point C which is at a level lower than A and AM is the horizontal line, the $\angle MAC$ is called the angle of depression.

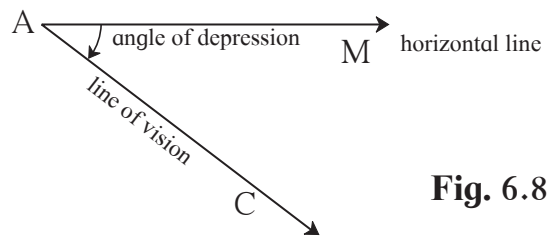


Fig. 6.8

When we see above the horizontal line, the angle formed is the angle of elevation. When we see below the horizontal line, the angle formed is the angle of depression.

Solved Examples

Ex. (1) An observer at a distance of 10 m from a tree looks at the top of the tree, the angle of elevation is 60° . What is the height of the tree ? ($\sqrt{3} = 1.73$)

Solution : In figure 6.9, $AB = h =$ height of the tree.

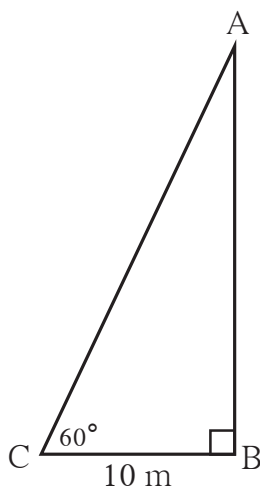


Fig. 6.9

$BC = 10$ m, distance of the observer from the tree .

Angle of elevation (θ) = $\angle BCA = 60^\circ$

from figure, $\tan\theta = \frac{AB}{BC}$ (I)

$\tan 60^\circ = \sqrt{3}$ (II)

$\therefore \frac{AB}{BC} = \sqrt{3}$ from equation (I) and (II)

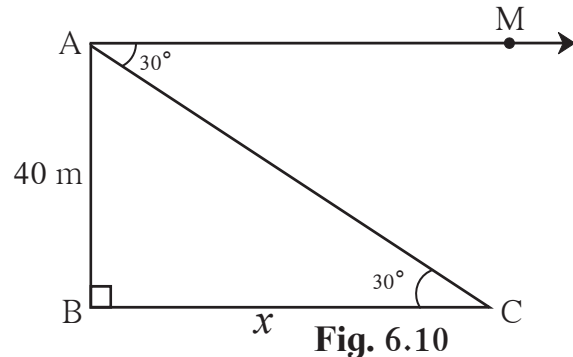
$\therefore AB = BC \sqrt{3} = 10\sqrt{3}$

$\therefore AB = 10 \times 1.73 = 17.3$ m

\therefore height of the tree is 17.3m.

Ex. (2) From the top of a building, an observer is looking at a scooter parked at some distance away, makes an angle of depression of 30° . If the height of the building is 40m, find how far the scooter is from the building. ($\sqrt{3} = 1.73$)

Solution: In the figure 6.10, AB is the building. A scooter is at C which is 'x' m away from the building. In figure, 'A' is the position of the observer.



AM is the horizontal line and $\angle MAC$ is the angle of depression.
 $\angle MAC$ and $\angle ACB$ are alternate angles.

from fig, $\tan 30^\circ = \frac{AB}{BC}$

$$\therefore \frac{1}{\sqrt{3}} = \frac{40}{x}$$

$$\begin{aligned} \therefore x &= 40\sqrt{3} \\ &= 40 \times 1.73 \\ &= 69.20 \text{ m.} \end{aligned}$$

\therefore the scooter is 69.20 m. away from the building.

Ex. (3) To find the width of the river, a man observes the top of a tower on the opposite bank making an angle of elevation of 61° . When he moves 50m backward from bank and observes the same top of the tower, his line of vision makes an angle of elevation of 35° . Find the height of the tower and width of the river. ($\tan 61^\circ = 1.8$, $\tan 35^\circ = 0.7$)

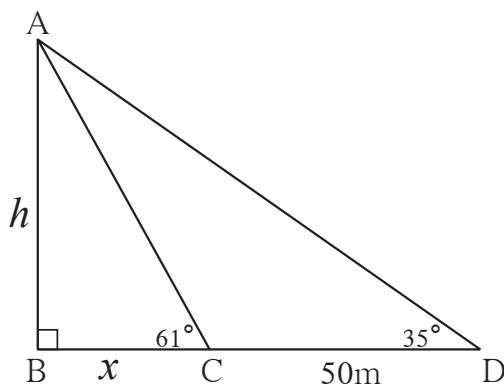


Fig. 6.11

Solution : seg AB shows the tower on the opposite bank. 'A' is the top of the tower and seg BC shows the width of the river. Let 'h' be the height of the tower and 'x' be the width of the river.

from figure, $\tan 61^\circ = \frac{h}{x}$

$$\therefore 1.8 = \frac{h}{x}$$

$$h = 1.8 \times x$$

$$10h = 18x \dots\dots\dots \text{(I)} \dots\dots \text{multiplying by 10}$$

In right angled ΔABD ,

$$\tan 35 = \frac{h}{x + 50}$$

$$0.7 = \frac{h}{x + 50}$$

$$\therefore h = 0.7(x + 50)$$

$$\therefore 10h = 7(x + 50) \dots\dots\dots \text{(II)}$$

\therefore from equations (I) and (II) ,

$$18x = 7(x + 50)$$

$$\therefore 18x = 7x + 350$$

$$\therefore 11x = 350$$

$$\therefore x = \frac{350}{11} = 31.82$$

$$\text{Now, } h = 1.8x = 1.8 \times 31.82$$

$$= 57.28 \text{ m.}$$

\therefore width of the river = 31.82 m and height of tower = 57.28 m

Ex. (4) Roshani saw an eagle on the top of a tree at an angle of elevation of 61° , while she was standing at the door of her house. She went on the terrace of the house so that she could see it clearly. The terrace was at a height of 4m. While observing the eagle from there the angle of elevation was 52° . At what height from the ground was the eagle ?
(Find the answer correct upto nearest integer)

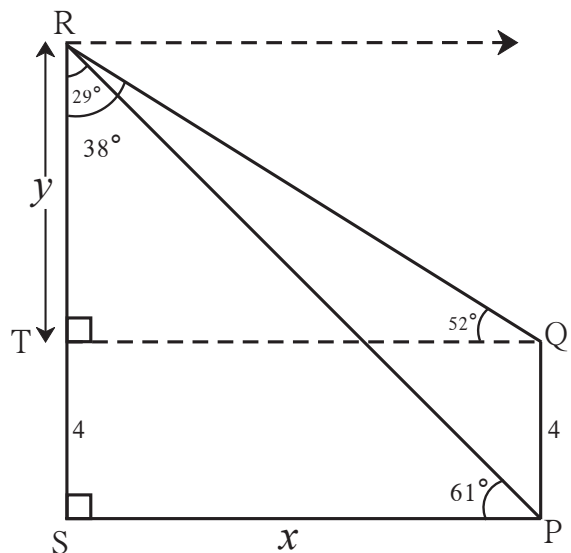


Fig. 6.12

$$(\tan 61^\circ = 1.80, \tan 52^\circ = 1.28, \tan 29^\circ = 0.55, \tan 38^\circ = 0.78)$$

Solution : In figure 6.12, PQ is the house and SR is the tree. The eagle is at R.

Draw seg QT \perp seg RS.

\therefore \square TSPQ is a rectangle.

Let SP = x and TR = y

Now in Δ RSP, \angle PRS = $90^\circ - 61^\circ = 29^\circ$

and in Δ RTQ, \angle QRT = $90^\circ - 52^\circ = 38^\circ$

$$\therefore \tan \angle PRS = \tan 29^\circ = \frac{SP}{RS}$$

$$\therefore 0.55 = \frac{x}{y+4}$$

$$\therefore x = 0.55(y + 4) \dots\dots\dots (I)$$

Similarly, $\tan \angle QRT = \frac{TQ}{RT}$

$$\therefore \tan 38^\circ = \frac{x}{y} \dots\dots\dots [\because SP = TQ = x]$$

$$\therefore 0.78 = \frac{x}{y}$$

$$\therefore x = 0.78y \dots\dots\dots (II)$$

$$\therefore 0.78y = 0.55(y + 4) \dots\dots\dots \text{from (I) and (II)}$$

$$\therefore 78y = 55(y + 4)$$

$$\therefore 78y = 55y + 220$$

$$\therefore 23y = 220$$

$$\therefore y = 9.565 = 10 \text{ (upto nearest integer)}$$

$$\therefore RS = y + 4 = 10 + 4 = 14$$

\therefore the eagle was at a height of 14 metre from the ground.

Ex. (5) A tree was broken due to storm. Its broken upper part was so inclined that its top touched the ground making an angle of 30° with the ground. The distance from the foot of the tree and the point where the top touched the ground was 10 metre. What was the height of the tree.

Solution: As shown in figure 6.13, suppose AB is the tree. It was broken at 'C' and its top touched at 'D'.

$\angle CDB = 30^\circ$, $BD = 10$ m, $BC = x$ m

$CA = CD = y$ m

In right angled $\triangle CDB$,

$$\tan 30^\circ = \frac{BC}{BD}$$

$$\frac{1}{\sqrt{3}} = \frac{x}{10}$$

$$x = \frac{10}{\sqrt{3}}$$

$$y = \frac{20}{\sqrt{3}}$$

$$x + y = \frac{10}{\sqrt{3}} + \frac{20}{\sqrt{3}}$$

$$= \frac{30}{\sqrt{3}}$$

$$x + y = 10\sqrt{3}$$

\therefore height of the tree was $10\sqrt{3}$ m.

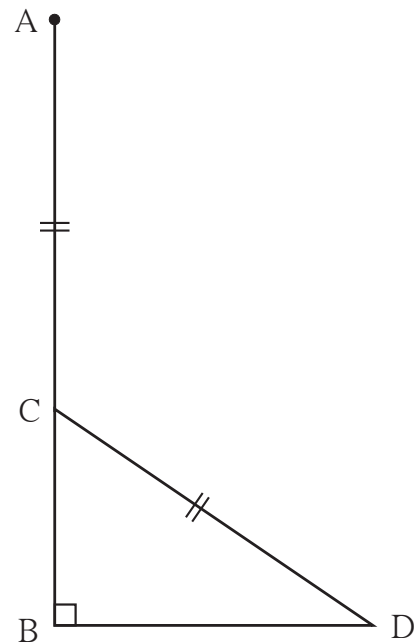


Fig. 6.13

Practice set 6.2

1. A person is standing at a distance of 80m from a church looking at its top. The angle of elevation is of 45° . Find the height of the church.
2. From the top of a lighthouse, an observer looking at a ship makes angle of depression of 60° . If the height of the lighthouse is 90 metre, then find how far the ship is from the lighthouse. ($\sqrt{3} = 1.73$)
3. Two buildings are facing each other on a road of width 12 metre. From the top of the first building, which is 10 metre high, the angle of elevation of the top of the second is found to be 60° . What is the height of the second building?
4. Two poles of heights 18 metre and 7 metre are erected on a ground. The length of the wire fastened at their tops is 22 metre. Find the angle made by the wire with the horizontal.
5. A storm broke a tree and the treetop rested 20 m from the base of the tree, making an angle of 60° with the horizontal. Find the height of the tree.
6. A kite is flying at a height of 60 m above the ground. The string attached to the kite is tied at the ground. It makes an angle of 60° with the ground. Assuming that the string is straight, find the length of the string. ($\sqrt{3} = 1.73$)

1. Choose the correct alternative answer for the following questions.

(1) $\sin\theta \operatorname{cosec}\theta = ?$

- (A) 1 (B) 0 (C) $\frac{1}{2}$ (D) $\sqrt{2}$

(2) $\operatorname{cosec}45^\circ = ?$

- (A) $\frac{1}{\sqrt{2}}$ (B) $\sqrt{2}$ (C) $\frac{\sqrt{3}}{2}$ (D) $\frac{2}{\sqrt{3}}$

(3) $1 + \tan^2\theta = ?$

- (A) $\cot^2\theta$ (B) $\operatorname{cosec}^2\theta$ (C) $\sec^2\theta$ (D) $\tan^2\theta$

(4) When we see at a higher level, from the horizontal line, angle formed is..... .

- (A) angle of elevation. (B) angle of depression.
 (C) 0 (D) straight angle.

2. If $\sin\theta = \frac{11}{61}$, find the values of $\cos\theta$ using trigonometric identity.

3. If $\tan\theta = 2$, find the values of other trigonometric ratios.

4. If $\sec\theta = \frac{13}{12}$, find the values of other trigonometric ratios.

5. Prove the following.

(1) $\sec\theta (1 - \sin\theta) (\sec\theta + \tan\theta) = 1$

(2) $(\sec\theta + \tan\theta) (1 - \sin\theta) = \cos\theta$

(3) $\sec^2\theta + \operatorname{cosec}^2\theta = \sec^2\theta \times \operatorname{cosec}^2\theta$

(4) $\cot^2\theta - \tan^2\theta = \operatorname{cosec}^2\theta - \sec^2\theta$

(5) $\tan^4\theta + \tan^2\theta = \sec^4\theta - \sec^2\theta$

(6) $\frac{1}{1 - \sin\theta} + \frac{1}{1 + \sin\theta} = 2 \sec^2\theta$

(7) $\sec^6 x - \tan^6 x = 1 + 3 \sec^2 x \times \tan^2 x$

(8) $\frac{\tan\theta}{\sec\theta + 1} = \frac{\sec\theta - 1}{\tan\theta}$

(9) $\frac{\tan^3\theta - 1}{\tan\theta - 1} = \sec^2\theta + \tan\theta$

