

5

Co-ordinate Geometry



Let's study.

- Distance formula
- Section formula
- Slope of a line



Let's recall.

We know how to find the distance between any two points on a number line. If co-ordinates of points P, Q and R are -1, -5 and 4 respectively then find the length of seg PQ, seg QR.

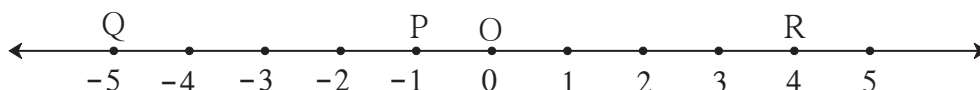


Fig. 5.1

If x_1 and x_2 are the co-ordinates of points A and B and $x_2 > x_1$ then length of seg AB = $d(A, B) = x_2 - x_1$

As shown in the figure, co-ordinates of points P, Q and R are -1, -5 and 4 respectively.

$$\therefore d(P, Q) = (-1) - (-5) = -1 + 5 = 4$$

$$\text{and } d(Q, R) = 4 - (-5) = 4 + 5 = 9$$

Using the same concept we can find the distance between two points on the same axis in XY-plane.



Let's learn.

(1) To find distance between any two points on an axis .

Two points on an axis are like two points on the number line. Note that points on the X-axis have co-ordinates such as $(2, 0)$, $(\frac{-5}{2}, 0)$, $(8, 0)$. Similarly points on the Y-axis have co-ordinates such as $(0, 1)$, $(0, \frac{17}{2})$, $(0, -3)$. Part of the X-axis which shows negative co-ordinates is OX' and part of the Y-axis which shows negative co-ordinates is OY' .

Activity:

In the figure, seg AB \parallel Y-axis and seg CB \parallel X-axis. Co-ordinates of points A and C are given.

To find AC, fill in the boxes given below.

ΔABC is a right angled triangle.

According to Pythagoras theorem,

$(AB)^2 + (BC)^2 = \square$

We will find co-ordinates of point B to find the lengths AB and BC,

CB \parallel X-axis \therefore y co-ordinate of B = \square

BA \parallel Y-axis \therefore x co-ordinate of B = \square

AB = $\square - \square = \square$

BC = $\square - \square = \square$

$\therefore AC^2 = \square + \square = \square$

$\therefore AC = \square$

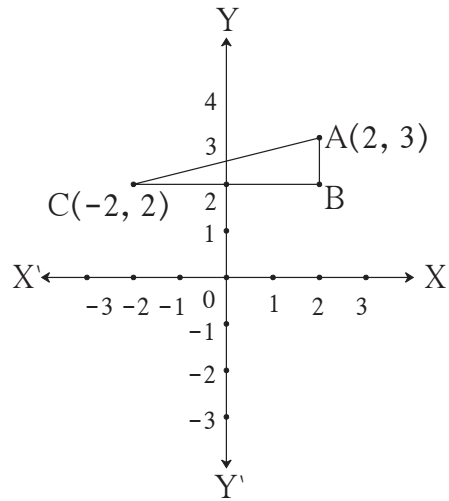


Fig. 5.6



Distance formula

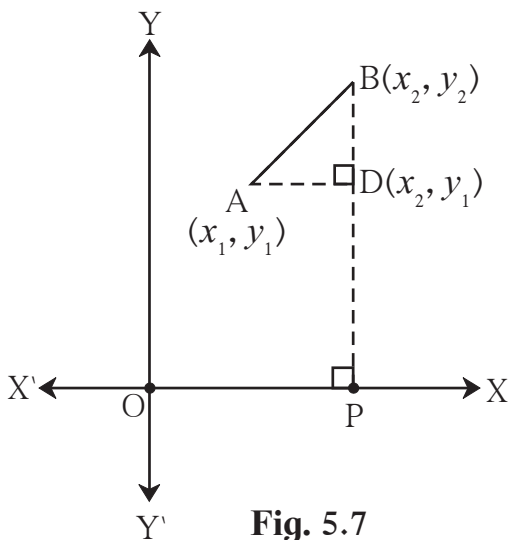


Fig. 5.7

In right angled triangle ΔABD ,

In the figure 5.7, $A(x_1, y_1)$ and $B(x_2, y_2)$ are any two points in the XY plane.

From point B draw perpendicular BP on X-axis. Similarly from point A draw perpendicular AD on seg BP.

seg BP is parallel to Y-axis.

\therefore the x co-ordinate of point D is x_2 .

seg AD is parallel to X-axis.

\therefore the y co-ordinate of point D is y_1 .

$\therefore AD = d(A, D) = x_2 - x_1$; $BD = d(B, D) = y_2 - y_1$

$AB^2 = AD^2 + BD^2$

$= (x_2 - x_1)^2 + (y_2 - y_1)^2$

$\therefore AB = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$

This is known as distance formula.

Note that, $\sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2} = \sqrt{(x_1 - x_2)^2 + (y_1 - y_2)^2}$

In the previous activity, we found the lengths of seg AB and seg AC and then used Pythagoras theorem to find the length of seg AC.

Now we will use distance formula to find AC.

A(2, 3) and C(-2, 2) is given

Let A(x_1, y_1) and C(x_2, y_2).

$x_1 = 2, y_1 = 3, x_2 = -2, y_2 = 2$

$$\begin{aligned} AC &= \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2} \\ &= \sqrt{(-2 - 2)^2 + (2 - 3)^2} \\ &= \sqrt{(-4)^2 + (-1)^2} \\ &= \sqrt{16 + 1} \\ &= \sqrt{17} \end{aligned}$$

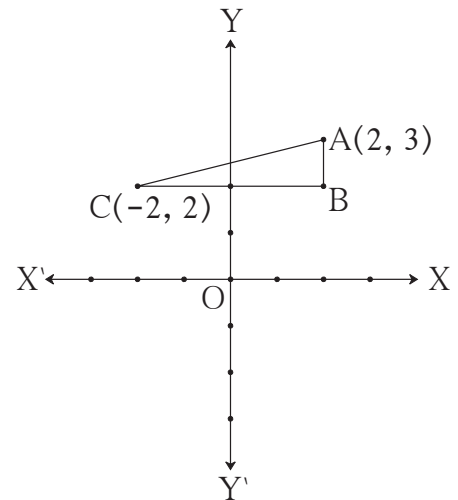


Fig. 5.8

seg AB || Y-axis and seg BC || X-axis.

∴ co-ordinates of point B are (2, 2).

∴ $AB = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2} = \sqrt{(2 - 2)^2 + (2 - 3)^2} = \sqrt{0 + 1} = 1$

$BC = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2} = \sqrt{(-2 - 2)^2 + (2 - 2)^2} = \sqrt{(-4)^2 + 0} = 4$

In the Figure 5.1, distance between points P and Q is found as $(-1) - (-5) = 4$. In XY- plane co-ordinates of these points are $(-1, 0)$ and $(-5, 0)$. Verify that, using the distance formula we get the same answer.



Remember this!

- Co-ordinates of origin are (0, 0). Hence if co-ordinates of point P are (x, y) then $d(O, P) = \sqrt{x^2 + y^2}$.
- If points P(x_1, y_1), Q(x_2, y_2) lie on the XY plane then $d(P, Q) = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$
that is, $PQ^2 = (x_2 - x_1)^2 + (y_2 - y_1)^2 = (x_1 - x_2)^2 + (y_1 - y_2)^2$

Ex. (7) If point (x, y) is equidistant from points $(7, 1)$ and $(3, 5)$, show that $y = x - 2$.

Solution : Let point $P(x, y)$ be equidistant from points $A(7, 1)$ and $B(3, 5)$

$$\therefore AP = BP$$

$$\therefore AP^2 = BP^2$$

$$\therefore (x - 7)^2 + (y - 1)^2 = (x - 3)^2 + (y - 5)^2$$

$$\therefore x^2 - 14x + 49 + y^2 - 2y + 1 = x^2 - 6x + 9 + y^2 - 10y + 25$$

$$\therefore -8x + 8y = -16$$

$$\therefore x - y = 2$$

$$\therefore y = x - 2$$

Ex. (8) Find the value of y if distance between points $A(2, -2)$ and $B(-1, y)$ is 5.

Solution : $AB^2 = [(-1) - 2]^2 + [y - (-2)]^2$ by distance formula

$$\therefore 5^2 = (-3)^2 + (y + 2)^2$$

$$\therefore 25 = 9 + (y + 2)^2$$

$$\therefore 16 = (y + 2)^2$$

$$\therefore y + 2 = \pm\sqrt{16}$$

$$\therefore y + 2 = \pm 4$$

$$\therefore y = 4 - 2 \text{ or } y = -4 - 2$$

$$\therefore y = 2 \text{ or } y = -6$$

$$\therefore \text{value of } y \text{ is } 2 \text{ or } -6.$$

Practice set 5.1

1. Find the distance between each of the following pairs of points.

(1) $A(2, 3), B(4, 1)$ (2) $P(-5, 7), Q(-1, 3)$ (3) $R(0, -3), S(0, \frac{5}{2})$

(4) $L(5, -8), M(-7, -3)$ (5) $T(-3, 6), R(9, -10)$ (6) $W(\frac{-7}{2}, 4), X(11, 4)$

2. Determine whether the points are collinear.

(1) $A(1, -3), B(2, -5), C(-4, 7)$ (2) $L(-2, 3), M(1, -3), N(5, 4)$

(3) $R(0, 3), D(2, 1), S(3, -1)$ (4) $P(-2, 3), Q(1, 2), R(4, 1)$

3. Find the point on the X-axis which is equidistant from $A(-3, 4)$ and $B(1, -4)$.

4. Verify that points $P(-2, 2), Q(2, 2)$ and $R(2, 7)$ are vertices of a right angled triangle.



Let's learn.

Section formula

In the figure 5.13, point P on the seg AB in XY plane, divides seg AB in the ratio $m : n$.

Assume $A(x_1, y_1)$ $B(x_2, y_2)$ and $P(x, y)$

Draw seg AC, seg PQ and seg BD perpendicular to X-axis.

$$\therefore C(x_1, 0); Q(x, 0)$$

and $D(x_2, 0)$.

$$\therefore \left. \begin{array}{l} CQ = x - x_1 \\ \text{and } QD = x_2 - x \end{array} \right\} \dots\dots\dots (I)$$

seg AC \parallel seg PQ \parallel seg BD.

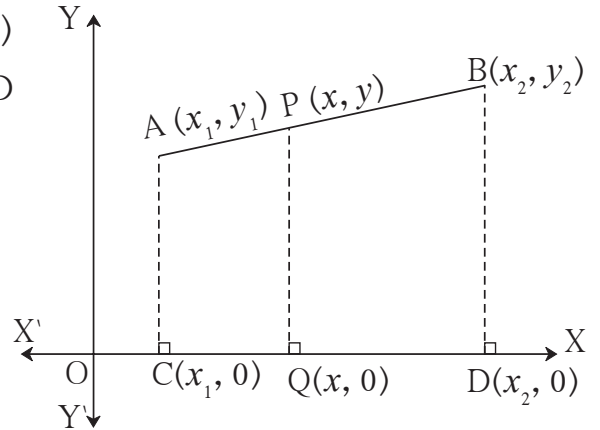


Fig. 5.13

\therefore By the property of intercepts of three parallel lines, $\frac{AP}{PB} = \frac{CQ}{QD} = \frac{m}{n}$

Now $CQ = x - x_1$ and $QD = x_2 - x$ from (I)

$$\therefore \frac{x - x_1}{x_2 - x} = \frac{m}{n}$$

$$\therefore n(x - x_1) = m(x_2 - x)$$

$$\therefore nx - nx_1 = mx_2 - mx$$

$$\therefore mx + nx = mx_2 + nx_1$$

$$\therefore x(m + n) = mx_2 + nx_1$$

$$\therefore x = \frac{mx_2 + nx_1}{m + n}$$

Similarly drawing perpendiculars from points A, P and B to Y-axis,

we get, $y = \frac{my_2 + ny_1}{m + n}$.

\therefore co-ordinates of the point, which divides the line segment joining the

points $A(x_1, y_1)$ and $B(x_2, y_2)$ in the ratio $m : n$ are given by

$$\left(\frac{mx_2 + nx_1}{m + n}, \frac{my_2 + ny_1}{m + n} \right).$$

Co-ordinates of the midpoint of a segment

If $A(x_1, y_1)$ and $B(x_2, y_2)$ are two points and $P(x, y)$ is the midpoint of seg AB then $m = n$.

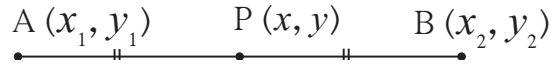


Fig. 5.14

\therefore values of x and y can be written as

$x = \frac{mx_2 + nx_1}{m + n}$ $= \frac{mx_2 + mx_1}{m + m} \quad \because m = n$ $= \frac{m(x_1 + x_2)}{2m}$ $= \frac{x_1 + x_2}{2}$	<div style="border-left: 1px dashed red; height: 100%;"></div>	$y = \frac{my_2 + ny_1}{m + n}$ $= \frac{my_2 + my_1}{m + m} \quad \because m = n$ $= \frac{m(y_1 + y_2)}{2m}$ $= \frac{y_1 + y_2}{2}$
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\therefore co-ordinates of midpoint P are $\left(\frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2}\right)$

This is called as **midpoint formula**.

In the previous standard we have shown that $\frac{a+b}{2}$ is the midpoint of the segment joining two points indicating rational numbers a and b on a number line. Note that it is a special case of the above midpoint formula.

***** Solved Examples *****

Ex. (1) If $A(3,5)$, $B(7,9)$ and point Q divides seg AB in the ratio $2:3$ then find co-ordinates of point Q .

Solution : In the given example let $(x_1, y_1) = (3, 5)$

and $(x_2, y_2) = (7, 9)$.

$$m : n = 2 : 3$$

According to section formula,

$$x = \frac{mx_2 + nx_1}{m + n} = \frac{2 \times 7 + 3 \times 3}{2 + 3} = \frac{23}{5} \qquad y = \frac{my_2 + ny_1}{m + n} = \frac{2 \times 9 + 3 \times 5}{2 + 3} = \frac{33}{5}$$

\therefore Co-ordinates of Q are $\left(\frac{23}{5}, \frac{33}{5}\right)$

∴ co-ordinates of point D are $x = \frac{x_2 + x_3}{2}$, $y = \frac{y_2 + y_3}{2}$ midpoint theorem

Point G(x, y) is centroid of triangle ΔABC . ∴ AG : GD = 2 : 1

∴ according to section formula,

$$x = \frac{2\left(\frac{x_2 + x_3}{2}\right) + 1 \times x_1}{2 + 1} = \frac{x_2 + x_3 + x_1}{3} = \frac{x_1 + x_2 + x_3}{3}$$

$$y = \frac{2\left(\frac{y_2 + y_3}{2}\right) + 1 \times y_1}{2 + 1} = \frac{y_2 + y_3 + y_1}{3} = \frac{y_1 + y_2 + y_3}{3}$$

Thus if (x_1, y_1) , (x_2, y_2) and (x_3, y_3) are the vertices of a triangle then the co-ordinates of the centroid are $\left(\frac{x_1 + x_2 + x_3}{3}, \frac{y_1 + y_2 + y_3}{3}\right)$.

This is called the **centroid formula**.



Remember this!

- Section formula

The co-ordinates of a point which divides the line segment joined by two distinct points (x_1, y_1) and (x_2, y_2) in the ratio $m : n$ are $\left(\frac{mx_2 + nx_1}{m + n}, \frac{my_2 + ny_1}{m + n}\right)$.

- Midpoint formula

The co-ordinates of midpoint of a line segment joining two distinct points (x_1, y_1) and (x_2, y_2) are $\left(\frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2}\right)$.

- Centroid formula

If (x_1, y_1) , (x_2, y_2) and (x_3, y_3) are the vertices of a triangle then co-ordinates of the centroid are $\left(\frac{x_1 + x_2 + x_3}{3}, \frac{y_1 + y_2 + y_3}{3}\right)$.

***** Solved Examples *****

Ex. (1) If point T divides the segment AB with A(-7,4) and B(-6,-5) in the ratio 7:2, find the co-ordinates of T.

Solution : Let the co-ordinates of T be (x, y).

∴ by the section formula,

$$x = \frac{mx_2 + nx_1}{m+n} = \frac{7 \times (-6) + 2 \times (-7)}{7+2}$$

$$= \frac{-42 - 14}{9} = \frac{-56}{9}$$

$$y = \frac{my_2 + ny_1}{m+n} = \frac{7 \times (-5) + 2 \times (4)}{7+2}$$

$$= \frac{-35 + 8}{9} = \frac{-27}{9} = -3$$

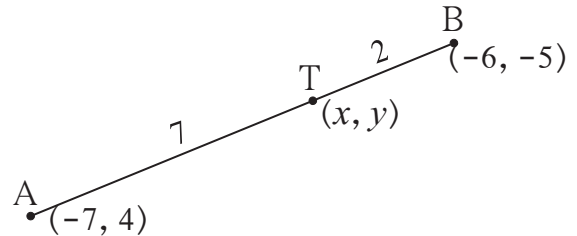


Fig. 5.17

∴ co-ordinates of point T are $\left(\frac{-56}{9}, -3\right)$.

Ex. (2) If point P(-4, 6) divides the line segment AB with A(-6, 10) and B(r, s) in the ratio 2:1, find the co-ordinates of B.

Solution : By section formula

$-4 = \frac{2 \times r + 1 \times (-6)}{2 + 1}$ $\therefore -4 = \frac{2r - 6}{3}$ $\therefore -12 = 2r - 6$ $\therefore 2r = -6$ $\therefore r = -3$	<div style="border-left: 1px dashed red; height: 100%;"></div>	$6 = \frac{2 \times s + 1 \times 10}{2 + 1}$ $\therefore 6 = \frac{2s + 10}{3}$ $\therefore 18 = 2s + 10$ $\therefore 2s = 8$ $\therefore s = 4$
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∴ co-ordinates of point B are (-3, 4).

Ex. (3) A(15,5), B(9,20) and A-P-B. Find the ratio in which point P(11,15) divides segment AB.

Solution : Suppose, point P(11,15) divides segment AB in the ratio $m : n$

∴ by section formula,

$$x = \frac{mx_2 + nx_1}{m+n}$$

$$\therefore 11 = \frac{9m+15n}{m+n}$$

$$\therefore 11m + 11n = 9m + 15n$$

$$\therefore 2m = 4n$$

$$\therefore \frac{m}{n} = \frac{4}{2} = \frac{2}{1}$$

\therefore The required ratio is 2 : 1.

Similarly, find the ratio using y co-ordinates. Write the conclusion.

Ex. (4) Find the co-ordinates of the points of trisection of the segment joining the points A (2,-2) and B(-7,4) .

(The two points that divide the line segment in three equal parts are called as points of trisection of the segment.)

Solution : Let points P and Q be the points of trisection of the line segment joining the points A and B.

Point P and Q divide line segment AB into three parts.

$$AP = PQ = QB \dots\dots\dots (I)$$

$$\frac{AP}{PB} = \frac{AP}{PQ+QB} = \frac{AP}{AP+AP} = \frac{AP}{2AP} = \frac{1}{2} \dots\dots\dots \text{From (I)}$$

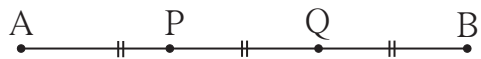


Fig. 5.18

Point P divides seg AB in the ratio 1:2.

$$x \text{ co-ordinate of point P} = \frac{1 \times (-7) + 2 \times 2}{1+2} = \frac{-7+4}{3} = \frac{-3}{3} = -1$$

$$y \text{ co-ordinate of point P} = \frac{1 \times 4 + 2 \times (-2)}{1+2} = \frac{4-4}{3} = \frac{0}{3} = 0$$

$$\text{Point Q divides seg AB in the ratio 2:1. } \therefore \frac{AQ}{QB} = \frac{2}{1}$$

$$x \text{ co-ordinate of point Q} = \frac{2 \times (-7) + 1 \times 2}{2+1} = \frac{-14+2}{3} = \frac{-12}{3} = -4$$

$$y \text{ co-ordinate of point Q} = \frac{2 \times 4 + 1 \times (-2)}{2+1} = \frac{8-2}{3} = \frac{6}{3} = 2$$

\therefore co-ordinates of points of trisection are (-1, 0) and (-4, 2).

For more information :

See how the external division of the line segment joining points A and B takes place.

Let us see how the co-ordinates of point P can be found out if P divides the line segment joining points A(-4, 6) and B(5, 10) in the ratio 3:1 externally.

$$\frac{AP}{PB} = \frac{3}{1} \text{ that is AP is larger than PB and A-B-P.}$$

$$\frac{AP}{PB} = \frac{3}{1} \text{ that is AP} = 3k, \text{BP} = k, \text{then AB} = 2k$$

$$\therefore \frac{AB}{BP} = \frac{2}{1}$$

Now point B divides seg AP in the ratio 2 : 1.

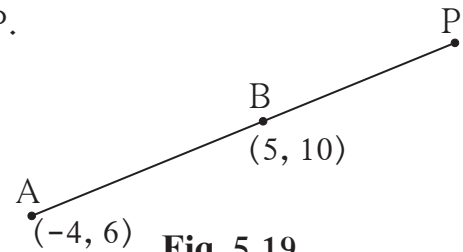


Fig. 5.19

We have learnt to find the coordinates of point P if co-ordinates of points A and B are known.

Practice set 5.2

1. Find the coordinates of point P if P divides the line segment joining the points A(-1,7) and B(4,-3) in the ratio 2 : 3.
2. In each of the following examples find the co-ordinates of point A which divides segment PQ in the ratio $a : b$.
 - (1) P(-3, 7), Q(1, -4), $a : b = 2 : 1$
 - (2) P(-2, -5), Q(4, 3), $a : b = 3 : 4$
 - (3) P(2, 6), Q(-4, 1), $a : b = 1 : 2$
3. Find the ratio in which point T(-1, 6) divides the line segment joining the points P(-3, 10) and Q(6, -8).
4. Point P is the centre of the circle and AB is a diameter . Find the coordinates of point B if coordinates of point A and P are (2, -3) and (-2, 0) respectively.
5. Find the ratio in which point P(k, 7) divides the segment joining A(8, 9) and B(1, 2). Also find k .
6. Find the coordinates of midpoint of the segment joining the points (22, 20) and (0, 16).
7. Find the centroids of the triangles whose vertices are given below.
 - (1) (-7, 6), (2, -2), (8, 5)
 - (2) (3, -5), (4, 3), (11, -4)
 - (3) (4, 7), (8, 4), (7, 11)

Here $\theta = 45^\circ$.

Use slope, $m = \tan\theta$ and verify that slopes of parallel lines are equal.

Similarly taking $\theta = 30^\circ$, $\theta = 60^\circ$ verify that slopes of parallel lines are equal.



Remember this!

The slope of X- axis and of any line parallel to X- axis is zero.

The slope of Y- axis and of any line parallel to Y- axis cannot be determined.

Solved Examples

EX. (1) Find the slope of the line passing through the points A (-3, 5), and B (4, -1)

Solution : Let, $x_1 = -3$, $x_2 = 4$, $y_1 = 5$, $y_2 = -1$

$$\therefore \text{Slope of line AB} = \frac{y_2 - y_1}{x_2 - x_1} = \frac{-1 - 5}{4 - (-3)} = \frac{-6}{7}$$

EX. (2) Show that points P(-2, 3), Q(1, 2), R(4, 1) are collinear.

Solution : P(-2, 3), Q(1, 2) and R(4, 1) are given points

$$\text{slope of line PQ} = \frac{y_2 - y_1}{x_2 - x_1} = \frac{2 - 3}{1 - (-2)} = -\frac{1}{3}$$

$$\text{Slope of line QR} = \frac{y_2 - y_1}{x_2 - x_1} = \frac{1 - 2}{4 - 1} = -\frac{1}{3}$$

Slope of line PQ and line QR is equal.

But point Q lies on both the lines.

\therefore Point P, Q, R are collinear.

EX. (3) If slope of the line joining points P(k, 0) and Q(-3, -2) is $\frac{2}{7}$ then find k.

Solution : P(k, 0) and Q(-3, -2)

$$\text{Slope of line PQ} = \frac{-2 - 0}{-3 - k} = \frac{-2}{-3 - k}$$

But slope of line PQ is given to be $\frac{2}{7}$.

$$\therefore \frac{-2}{-3 - k} = \frac{2}{7} \quad \therefore k = 4$$

EX. (4) If A (6, 1), B (8, 2), C (9, 4) and D (7, 3) are the vertices of \square ABCD , show that \square ABCD is a parallelogram.

Solution : You know that Slope of line = $\frac{y_2 - y_1}{x_2 - x_1}$

$$\text{Slope of line AB} = \frac{2-1}{8-6} = \frac{1}{2} \dots\dots\dots \text{(I)}$$

$$\text{Slope of line BC} = \frac{4-2}{9-8} = 2 \dots\dots\dots \text{(II)}$$

$$\text{Slope of line CD} = \frac{3-4}{7-9} = \frac{1}{2} \dots\dots\dots \text{(III)}$$

$$\text{Slope of line DA} = \frac{3-1}{7-6} = 2 \dots\dots\dots \text{(IV)}$$

Slope of line AB = Slope of line CD From (I) and (III)

\therefore line AB \parallel line CD

Slope of line BC = Slope of line DA From (II) and (IV)

\therefore line BC \parallel line DA

Both the pairs of opposite sides of the quadrilateral are parallel

\therefore \square ABCD is a parallelogram.

Practice set 5.3

1. Angles made by the line with the positive direction of X-axis are given. Find the slope of these lines.
 (1) 45° (2) 60° (3) 90°
2. Find the slopes of the lines passing through the given points.
 (1) A (2, 3) , B (4, 7) (2) P (-3, 1) , Q (5, -2)
 (3) C (5, -2) , D (7, 3) (4) L (-2, -3) , M (-6, -8)
 (5) E(-4, -2) , F (6, 3) (6) T (0, -3) , S (0, 4)
3. Determine whether the following points are collinear.
 (1) A(-1, -1), B(0, 1), C(1, 3) (2) D(-2, -3), E(1, 0), F(2, 1)
 (3) L(2, 5), M(3, 3), N(5, 1) (4) P(2, -5), Q(1, -3), R(-2, 3)
 (5) R(1, -4), S(-2, 2), T(-3, 4) (6) A(-4, 4), K(-2, $\frac{5}{2}$), N(4, -2)
4. If A (1, -1), B (0, 4), C (-5, 3) are vertices of a triangle then find the slope of each side.
5. Show that A (-4, -7), B (-1, 2), C (8, 5) and D (5, -4) are the vertices of a parallelogram.

6. Find k , if $R(1, -1)$, $S(-2, k)$ and slope of line RS is -2 .
7. Find k , if $B(k, -5)$, $C(1, 2)$ and slope of the line is 7 .
8. Find k , if $PQ \parallel RS$ and $P(2, 4)$, $Q(3, 6)$, $R(3, 1)$, $S(5, k)$.

Problem set 5

1. Fill in the blanks using correct alternatives.

(1) Seg AB is parallel to Y -axis and coordinates of point A are $(1, 3)$ then co-ordinates of point B can be

- (A) $(3, 1)$ (B) $(5, 3)$ (C) $(3, 0)$ (D) $(1, -3)$

(2) Out of the following, point lies to the right of the origin on X - axis.

- (A) $(-2, 0)$ (B) $(0, 2)$ (C) $(2, 3)$ (D) $(2, 0)$

(3) Distance of point $(-3, 4)$ from the origin is

- (A) 7 (B) 1 (C) 5 (D) -5

(4) A line makes an angle of 30° with the positive direction of X - axis. So the slope of the line is

- (A) $\frac{1}{2}$ (B) $\frac{\sqrt{3}}{2}$ (C) $\frac{1}{\sqrt{3}}$ (D) $\sqrt{3}$

2. Determine whether the given points are collinear.

(1) $A(0, 2)$, $B(1, -0.5)$, $C(2, -3)$

(2) $P(1, 2)$, $Q(2, \frac{8}{5})$, $R(3, \frac{6}{5})$

(3) $L(1, 2)$, $M(5, 3)$, $N(8, 6)$

3. Find the coordinates of the midpoint of the line segment joining $P(0, 6)$ and $Q(12, 20)$.

4. Find the ratio in which the line segment joining the points $A(3, 8)$ and $B(-9, 3)$ is divided by the Y - axis.

5. Find the point on X -axis which is equidistant from $P(2, -5)$ and $Q(-2, 9)$.

6. Find the distances between the following points.

- (i) $A(a, 0)$, $B(0, a)$ (ii) $P(-6, -3)$, $Q(-1, 9)$ (iii) $R(-3a, a)$, $S(a, -2a)$

7. Find the coordinates of the circumcentre of a triangle whose vertices are $(-3, 1)$, $(0, -2)$ and $(1, 3)$

